

Revision for the 2<sup>nd</sup> small test on:.....

Oscillations:

Oscillator – a device able to freely to oscillate – make a periodic motion  
(a spring oscillator, pendulum)

**Period:**

T – time needed to make one complete cycle (s)

**Frequency:**

f - gives number of complete cycles per a time (s-1)

- if the time is given in seconds, frequency is measured in s-1 – Hz (hertz)
- there might be frequency given in revs per minute (revs/min)
- $f = 1/T$  (kilohertz – 1 kHz = 10<sup>3</sup> Hz, megahertz – 1 MHz = 10<sup>6</sup> Hz)

- A heart makes beats 75 times per minute. Calculate frequency and period of human heart.
- A body oscillating on a spring – deflections from the equilibrium – y (m).
- A maximum of deflections – amplitude – y<sub>m</sub> (m).

$$y = y_m \sin \varphi = y_m \sin \omega t$$

$$\omega = 2\pi / T = 2\pi f \quad (\omega - \text{angular frequency}) \text{ (rad.s-1)}$$

**Velocity and acceleration of oscillations**

$$a_0 = -\omega^2 y$$

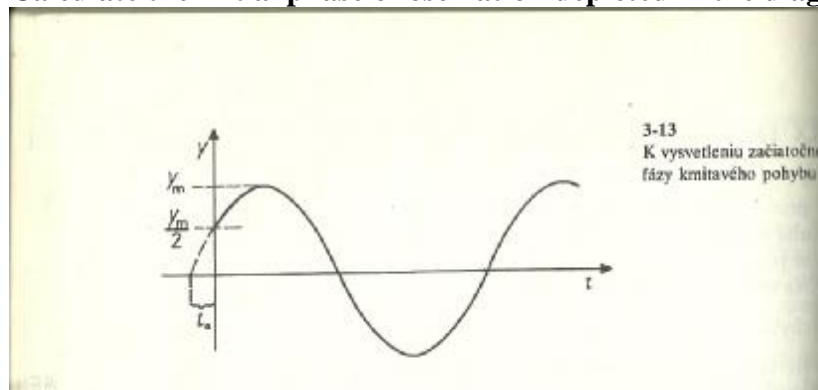
$$v_0 = \omega r$$

- **A point object oscillates with amplitude of 0.2 m. Calculate deflection of the point object at  $\frac{1}{4} T$ ,  $\frac{1}{3} T$ ,  $\frac{1}{2} T$ . Use  $y = y_m \sin \omega t$ .**
- **Harmonic oscillation is described by  $y = 8 \sin 4\pi t$  cm. Calculate amplitude and frequency of the oscillator.**
- **What is the time needed to reach deflection of - 8 cm for an oscillator described by equation  $y = 8 \sin 4\pi t$  cm?**

**Phase of oscillations**

- $y = y_m \sin \varphi = y_m \sin (\omega t + \varphi)$
- $\varphi$  – initial phase

**Calculate the initial phase of oscillation depicted in the diagram:**



- Calculate initial phase of the harmonic oscillation which is in equilibrium in time  $t = T/8$ . Write equation of the oscillation.

### Dynamics of oscillations

$$F = F_G - F_P = m g - k (\Delta l + y) = - k y$$

$k$  – spring constant (N.m-1)

$$a = F / m = - k y / m$$

$$\omega_0^2 = k / m$$

$$\omega_0 = \sqrt{k / m}$$

$$T = 2\pi \sqrt{m / k} \text{ (s)}$$

$$f = (1 / 2\pi) \sqrt{k / m} \text{ (Hz)}$$

- There is a body hanging on a spring of a mass of 10 kg, which extension is 15cm. Calculate period of an oscillator.

### Energy of an oscillator

Work done by oscillator:

$$W = \frac{1}{2} F y = \frac{1}{2} k y^2$$

### Comparison

#### Mechanic oscillator

- n deflection –  $y$
- n velocity –  $v$
- n PE:  $E_p = \frac{1}{2} k y^2$
- n KE:  $E_k = \frac{1}{2} m v^2$
- n force –  $F$
- n mass –  $m$
- n spring constant –  $k = F/y$
- n period:  $T = 2\pi\sqrt{m/k}$

#### Electromagnetic oscillator

- n charge –  $Q$
- n current –  $I$
- n Electric energy:  $E_e = \frac{1}{2} Q U$   
 $= \frac{1}{2} Q^2 / C$  ( $C = Q/U$ )
- n Magnetic energy:  
 $E_m = \frac{1}{2} L I^2$
- n p.d.
- n inductance
- n  $1/C$  ( $C$  – capacity)
- n  $T = 2\pi\sqrt{LC}$  (Thomson's formula)

- Calculate period of the oscillations of the circuit with parameters:
  - a)  $C = 50 \mu\text{F}$  (micro farad),  $L = 50 \text{ H}$
  - b)  $C = 0.2 \mu\text{F}$ ,  $L = 0.79 \text{ H}$
  - c)  $C = 6 \text{ nF}$ ,  $L = 11 \mu\text{H}$

In which case can we hear the oscillations? (16 Hz – 20 kHz)